

Control system theory

Introduction to PID controllers

Need for control system

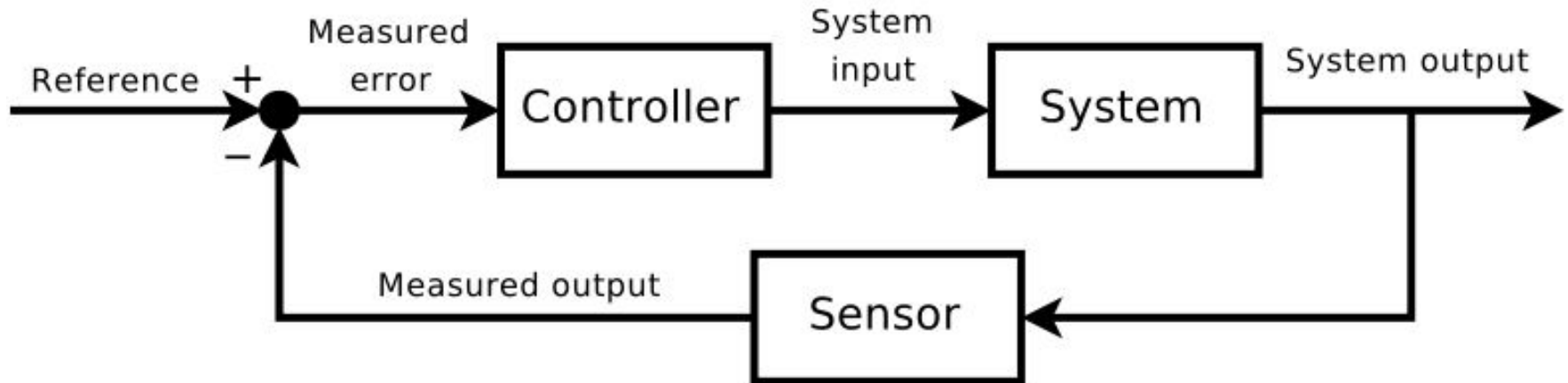
<https://www.youtube.com/watch?v=TOl0ZPexRhl#t=33s>

https://www.youtube.com/watch?v=Z0v-G0oo_FQ&index=4&list=PL2uH4qIrAkdoFWEr8cQ96JnnH4ms-DCvB

<https://www.youtube.com/watch?v=HfiHOpv6Htl&list=PL2uH4qIrAkdoFWEr8cQ96JnnH4ms-DCvB&index=7>

Controllers

Controllers deal with controlling a dynamic system. The objective of the control is to get a desired output from the system, given some constraints, ensuring stability.

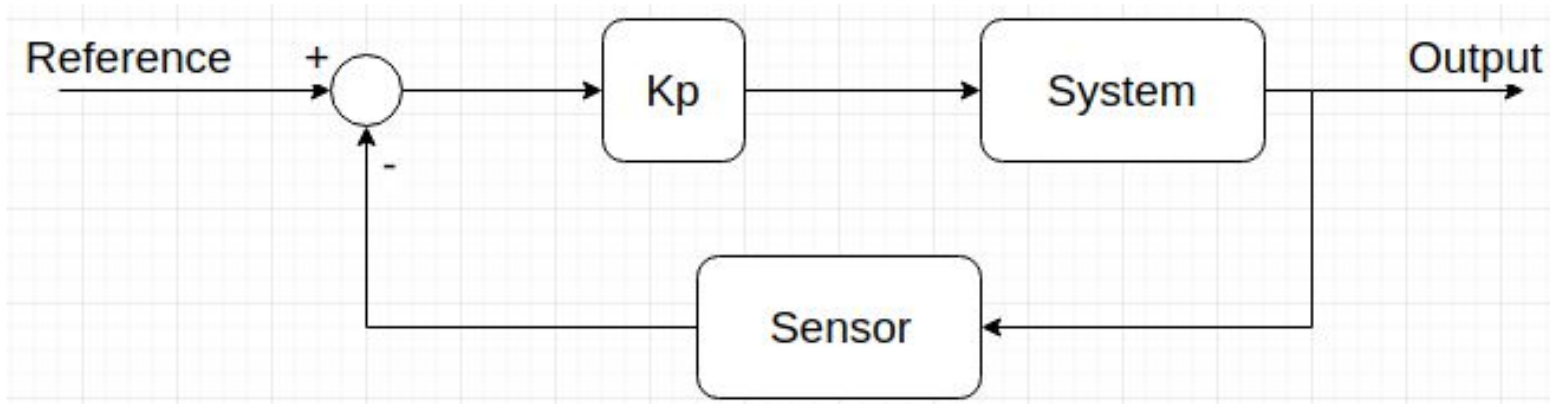


Different controllers

- P controller
- PI controller
- PD controller
- PID controller

Proportional(P) controller

In the Proportional only mode, the controller simply multiplies the error by the Proportional Gain (K_p) to get the controller output.



Advantages and drawbacks of P Control

Advantages

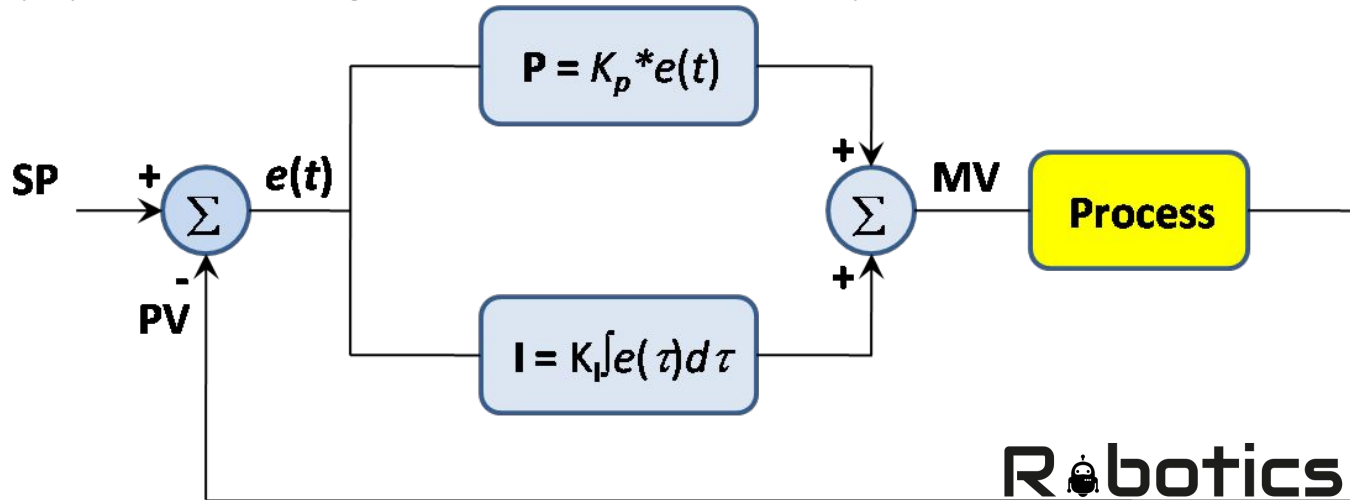
- Easy to implement
- Less computation resources required

Drawbacks

- Oscillations in the output might be present
- Steady state error is not zero
- Maximum overshoot is high

Proportional integral (PI) controller

In the PI only mode, the controller multiplies the error by the Proportional Gain (K_p) and adds integral of error to proportional term. Integral term makes sure that the steady state error is zero.



Advantages and drawbacks of PI controller

Advantages

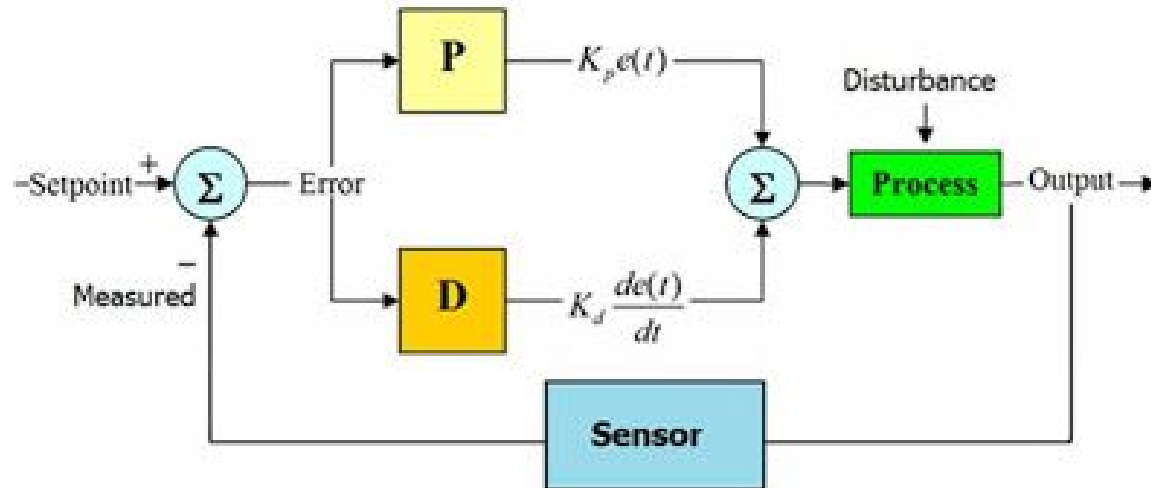
- Steady state error is zero

Drawbacks:

- Requires timer to keep track of time
- Tuning is difficult

PD controller

In the PI only mode, the controller multiplies the error by the Proportional Gain (K_p) and adds integral of error to proportional term.



Advantages and drawbacks

Advantages

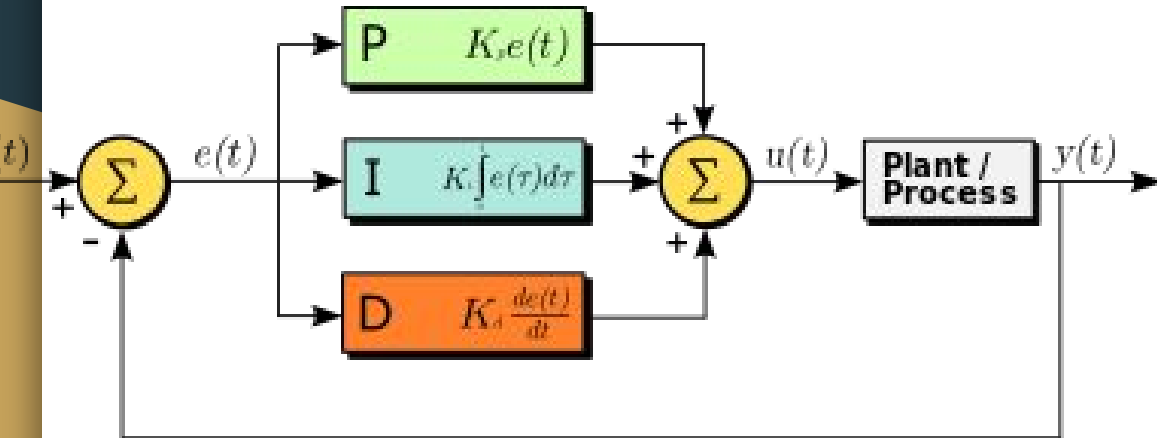
- Minimises the maximum overshoot
- Fast response

Drawbacks

- Steady state error is not guaranteed to be zero
- Amplifies noise signals

Proportional Integral Derivative (PID) controller

PID controller packs the benefits of all of the above controller.



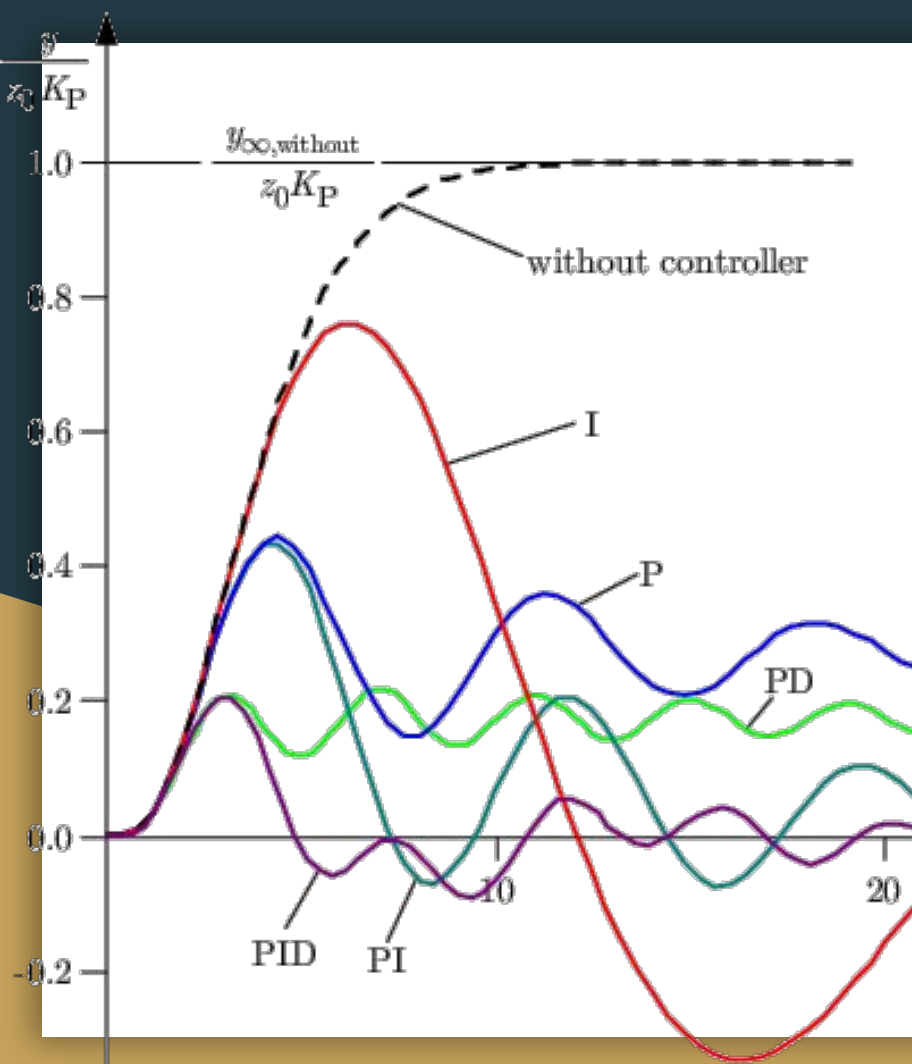
Advantages and drawbacks

Advantages:

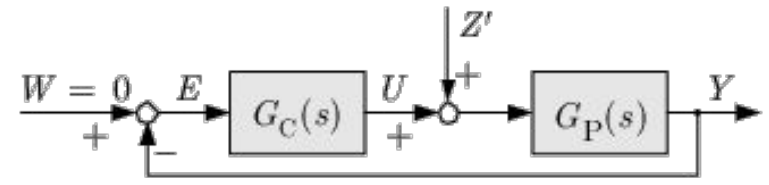
- No steady state error
- Low maximum overshoot

Drawbacks:

- Difficult to implement
- Gain tuning is a difficult task



Controller	$\frac{M_p}{z_0 K_P}$	$\frac{t_p}{T}$	z_{∞}	$K_{C_{opt}}$	$\frac{T_{opt}}{4T}$	$\frac{T_{D_{opt}}}{4T}$
PID	0.20	19	—	2.74	0.22	0.67
PI	0.44	35	—	2.45	1.38	—
PD	0.22	31	-0.17	4.74	—	0.32
P	0.45	22	-0.27	2.68	—	—
I	0.76	40	—	—	$0.88 \cdot K_P$	—



Demonstration

<https://www.youtube.com/watch?v=fusr9eTceEo>

<https://sites.google.com/site/fpgaandco/pid>

References

- Robotics club, IITK lecture on PID(2016-17)
- [http://www.ee.ic.ac.uk/pcheung/teaching/DE2_EE/Lecture%2017%20-%20PID%20controller%20\(notes%20x1\).pdf](http://www.ee.ic.ac.uk/pcheung/teaching/DE2_EE/Lecture%2017%20-%20PID%20controller%20(notes%20x1).pdf)
- <https://www.youtube.com/watch?v=UR0hOmjaHp0>
- <https://www.youtube.com/watch?v=XfAt6hNV8XM>